

## SantGadgeBabaAmravatiUniversity,Amravati

Faculty of Science and Technology Programme: **M.Sc. II Statistics (NEP)**

### Program Outcomes (POs)

At the end of the programme, students would be able to

**PO1: Critical Thinking:** Think critically for data driven solution with advanced Methodology. Students may be able to think critically everything around him/her. They will be able to take better action in any critical situation in their life.

**PO2:** Nurture their curious minds toward translation and application & Statistical knowledge to find solutions to real world problems.

**PO3: Employability:** get knowledge and skills in depth necessary for employability of students in industry, Govt Sector and organizations as well as in academics.

**PO4: Empowerment:** be empowered to investigate, solve questions for which answer lies beyond the boundaries of conventional thinking.

**PO5: Effective decision making:** take proper decision in critical and complicated situations. Reduce risk factor and be able to maximize project.

**PO6: Effective citizenship:** get acquainted with the needs of the industry and society, and they become the assets for the society.

**PO7: Social interaction:** Develop sensitivity for social issues and become productive citizen of nation.

### Program Specific Outcomes (PSOs)

Upon completion of the programme successfully, students would be able to

**PSO1:** understand basic theoretical and applied principles of Statistics needed to enter the job force. They will be able to communicate key statistical concepts to non-statisticians. They also gain proficiency in using statistical ideas/principles for data analysis.

**PSO2:** groom as the next generation statisticians ready for scientific decision making, aided with advanced statistical software translating into sharp and extensive analytics pertinent to various domains.

**PSO3:** start consultancy for statistical analysis and can be helpful in interdisciplinary research.

**PSO4:** perform Statistical quality control, which is the most important sector of any industry where students can work as statisticians to approve the quality.

### **Employability Potential of the programme**

The programme offers many opportunities, where statisticians can work. By completing this programme, students are able to:

- Analyse things
- Understand patterns in them by asking different questions to it
- Compete with the current demand of the field

- To solve a specific problem

This “skill” is a key requirement for many analyst-type jobs like,

1. Statisticians
2. Business Analyst
3. Mathematician
4. Professor
5. Risk Analyst
6. Data Analyst
7. Content Analyst
8. Statistic Trainer

Besides all these students can work in various banking sector. Students can also work in government sector:

- Indian statistical services (ISS)
  - Staff selection services (SSC)
  - Reserve Bank of India (Junior statistical officer)
- By taking the programme, students are able to:

- Analyse numbers
- Understand patterns in them by asking different questions to it
- Go about it in a systematic fashion
- To solve a specific problem

This “skill” is a key requirement for many analyst-type jobs.

### **Career Options:**

**Data Analytics #1:** Students could get into any Analytics firm, and can assist customers in getting patterns out of data.

**Data Analytics #2:** For Data Analytics in banks, there can be algorithms developed for fraud deduction using the digital imprints. This requires analyzing large amounts of data. That could be a career choice - Digital Forensics.

**Market Research:** For doing a survey for customer expectations and behaviors, students utilize the data from online and offline channels to draw meaningful, actionable conclusions. For this the students need to use the various statistical methods which they learnt. So, Market Research in a MR firm or a corporate entity can be a large area of focus.

**Software Programmer:** With analytical bent of mind, Students could take up a software

programming job. It might not leverage learning but will leverage the “bent of mind” cultivated out of the education. Students could focus on areas like: Visual Representation of Data (Tableau, Quilk, PowerBI), Data Reporting (Crystal Reports)-that are aligned to the core skills.

**Government Statistician:** Our country requires a lot of econometric and statistical data for its running. Acreage, Yields, Health Statistics and the like. Bright young idealistic people are required to run our country too. Students could be a District Statistical Officer, who is in charge of collecting information from the district, analyzing it and sharing with the State Authorities.

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|-------------------------|---------------------|---|---------------------------------|
| <b>Semester<br/>III</b> | <b>Paper<br/>I</b>  | <b>Name of the paper<br/>Statistical Inference</b>    | <b>Subject code<br/>DSC I.3</b> |
|                         | <b>II</b>           | <b>Mathematical Programming</b>                       | <b>DSC II.3</b>                 |
|                         | <b>III</b>          | <b>Linear and nonlinear modeling</b>                  | <b>DSC III.3</b>                |
|                         | <b>IV</b>           | <b>Operations Research</b>                            | <b>DSEI.3</b>                   |
|                         |                     | <b>Bioassay</b>                                       | <b>DSEII.3</b>                  |
|                         |                     | <b>Econometrics</b>                                   | <b>DSE III.3</b>                |
|                         |                     | <b>Actuarial Statistics</b>                           | <b>DSE IV.3</b>                 |
|                         | <b>LAB I</b>        | <b>Practical I</b>                                    | <b>DSCI.3, DSC II.3</b>         |
| <b>LAB II</b>           | <b>Practical II</b> | <b>DSCIII.3, DSEI.3</b>                               |                                 |
| <b>Semester<br/>IV</b>  | <b>Paper<br/>I</b>  | <b>Name of the paper<br/>Computational Statistics</b> | <b>Subject code<br/>DSC I.4</b> |
|                         | <b>II</b>           | <b>Multivariate Analysis</b>                          | <b>DSC II.4</b>                 |
|                         | <b>III</b>          | <b>Stochastic Process</b>                             | <b>DSCIII.4</b>                 |
|                         | <b>IV</b>           | <b>Baysian Inference</b>                              | <b>DSEII.4</b>                  |
|                         |                     | <b>Statistical Ecology</b>                            | <b>DSE II.4</b>                 |
|                         |                     | <b>Regression Analysis</b>                            | <b>DSE II.4</b>                 |
|                         |                     | <b>Reliability Theory</b>                             | <b>DSE II.4</b>                 |
|                         | <b>Lab I</b>        | <b>Practical I</b>                                    | <b>DSC1.4, DSCII.4</b>          |
| <b>Lab II</b>           | <b>Practical II</b> | <b>DSC III.4,DSE II.4</b>                             |                                 |

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**M.Sc.II ( Statistics )(NEP Pattern) Semester III**  
**DSC I.3 : Statistical Inference**

**Course Objective**

The objective of estimation theory is to arrive at an estimator that exhibits optimality. To provide a systematic account of Neyman-Pearson theory of testing and closely related theory of point estimation and confidence sets, together with their applications.

**Course Outcome**

After completing this course, student is expected to learn the following:

- 1 Understand the various estimation and testing procedures to deal with real life problems.
- 2 Learn about the Fisher Information, lower bounds to variance of estimators, MVUE.
- 3 Understand the concept of Neyman-Pearson fundamental lemma, UMP test and interval estimation.
- 4 Understand the concept of critical regions, likelihood ratio test with its asymptotic distribution.

**Unit I** : Criteria of a good estimator - unbiasedness, consistency, efficiency, sufficiency. Minimal sufficient statistic. Exponential and Pitman families of distributions. Cramer-Rao lower bound approach to obtain minimum variance unbiased estimator. Uniformly minimum variance unbiased estimator, Complete statistic, Rao-Blackwell theorem, Lehmann-Scheffe theorem.

**Unit II** : Method of moments, minimum chi-square estimation, maximum likelihood estimator and its properties, CAN & BAN estimators. Ancillary statistic and Basu's theorem. Simple and composite hypothesis, concept of critical regions, test functions, two types of error, power of the test, level of significance, Neyman-Pearson lemma, uniformly most powerful (UMP) tests.

**Unit III** : Types A, A1 critical regions, likelihood ratio test (LRT) with its asymptotic distribution, UMP tests for monotone likelihood ratio of family of distributions. Similar tests with Neyman structure, Construction of similar and UMPU tests through Neyman structure.

**Unit IV** : Confidence interval, construction of confidence intervals using pivotal, shortest expected length confidence interval, uniformly most accurate one-sided confidence interval and its relation to UMP test for one-sided null against one-sided alternative hypothesis.

### **Books Recommended**

1. Rohatgi, V.K. & Saleh, A.K. Md.E. (2015). An Introduction to Probability and Statistics, 3<sup>rd</sup> Edition. Wiley.
2. Lehmann, E.L. & Casella, G. (2014). Theory of Point Estimation, 2<sup>nd</sup> Edition. Springer.
3. Lehmann, E.L. & Romano, J.P. (2010). Testing Statistical Hypotheses, 3<sup>rd</sup> Edition. Springer.  
Casella, G. & Berger, R.L. (2013). Statistical Inference, 2<sup>nd</sup> Edition. Cengage Learning.

### **DSC II.3 : Mathematical Programming**

#### **Course Objectives:**

Optimization techniques have application in almost all disciplines. To get on optimum solution to the problem under given constraints is always challenging. To get the best solution to such problems, there are different methods depending on the problem and constraints. Various such problems and methods to solve them are part of this course.

#### **Course Outcomes:**

**At the end of the course, students become well versed with,**

1. To formulate and solve linear programming problem (LPP). They also learn various methods to solve LPP. Application of LPP in industry, management, transportation, assignment etc.
2. Sensitivity analysis of LPP by studying the effect of changes in coefficients of constraints on the solutions to the problem. They also learn the effect of any other changes in the constraints, addition of new constraint on the solution to the problem.
3. Pure and mixed integer linear programming problem and formulation of nonlinear programming problem and different methods to solve them.
4. The problem and different methods of solving two person zero sum game.

**Unit I :L. P. :** Simplex method, variants of simplex method, duality in L. P. duality theorem, complementary slackness theorem, dual simplex method, transportation & assignment problems, method of solving transportation & assignment problems. Dynamic Programming :Dynamic programming approach for solving optimization problems, forward &



backward recursion formula, minimum path problem, single additive  
 constraint & additively separable  
 return, single  
 multiplicative constraint & additively separable return, single additive constraint & multiplicatively  
 separable return, Goal Programming.

**Unit II** : Sensitivity analysis of L.P.: Changes  
 in R.H.S. constraint  $b_i$ , changes in cost coefficient  $c_j$ , changes in coefficient of  
 constraints  $a_{ij}$ , addition of new variables, addition of new constraints. I.L.P.P.: Pure & mixed  
 I.L.P.P., methods for solving pure &  
 mixed I.L.P.P. Gomory's cutting plane method, Branch & Bound technique.

**Unit III** :  
 N.L.P.P.: General N.L.P.P., convex & concave functions, test for concavity & convexity, local optimum,  
 global optimum, basic results for local optimum & global optimum, Lagrange's methods  
 for optimality, K.T. conditions, Q.P.P. Wolfe's & Beale's method for solving Q.P.P.

**Unit IV :**

Game theory: 2 person zero sum game, pure & mixed strategies, saddle point of a matrix game, matrix  
 game without saddle point, methods for solving matrix game without  
 saddle point,  $2 \times 2$ ,  $m \times n$ ,  $m \times 2$ ,  $2 \times n$  matrix games, dominance principle, use of dominance principle in  
 game theory, solving game problems by simplex method.

**Books Recommended**

1. S.M. Sinha : Mathematical Programming Theory and Methods Elsevier
2. Melvyn Jeter: Mathematical Programming An introduction to optimization Routledge  
 Taylor and Francis group
3. N.S. Kambo: Mathematical Programming Technique East West Press Pvt Ltd.
4. R.K. Gupta : Linear Programming Krishna Prakashan

### **DSCIII.3 : Linear and Non linearModelling**

#### **Course Objectives:**

Regression analysis is the most common statistical modelling approach used in dataanalysisanditisthe basisforadvancedstatisticalmodelling.

Theobjectiveofthiscourseistoimpartknowledgeabouttheusedifferentusefultoolsusedinregressionanalysis.Therelationshipbetweenvariables can be of different types like linear, nonlinear etc. The relationship is represented in terms of a model. Theadequacy of any model can be checked using residual plots and residual analysis.Appropriate statisticaltoolsarerequiredtocheckfortheviolationsofmodelassumptionsandfordealingwithproblemsof multicollinearityetc.

#### **Course Outcomes:**

**At theend ofthecourse,studentsbecomewellversed with,**

1. LinearandMultipleregression.
2. To interpret different types of plots such as residual plots, normal probability plotsetc. To check for the violations of model assumptions using residual analysis andotherstatisticaltests.
3. Todifferentiatebetweenlinearandnonlinearregressionundergivensituation.
4. GeneralizedLinearModelsincludinglogistic

**Unit I :**

:MultipleLinearregression:Modelassumptionsandcheckingfortheviolationsofmodelassumption  
., Residual analysis – definition of residuals, standardized residuals, residual plots,statistical  
tests on residuals, Press statistics. Transformation of variables, Box-Cox  
powertransformation.Outliers : Detection and remedial measures, Influential observations :  
leverage, measures ofinfluence,Cook’sD,DFITSANDDFBETAS.

**Unit II** :Multicollinearity : Concept and definition of M.C., sources of M.C. consequences of M.C.identificationofM.C.usingthecorrelationmatrix,VIFremedialmeasures(collectingaddition aldata,modelrespecification,),conceptofridge regression.Autocorrelation:consequences,Durbin -Watson test, Estimation of parameters in the presence of autocorrelation.

**Unit III** : Variable selection: Problem of variable selection, criteria for evaluation subset regression models (choosing subsets), coefficient of multiple determination, residual mean square, Mallows' Cp Statistics. Computational Techniques for variable selection-Forward selection, Backward elimination, stepwise regression.

Non-linear regression: Difference between Linear and Non-

Linear Regression Models, transformation to a linear model, Intrinsically linear and non-linear models. Parameter estimation using the Newton-Gauss method, Hypothesis testing.

**Unit IV** : Generalized linear models : Exponential families, Definition of GLM, Link function, Estimation of parameters and inference in GLM. Logistic regression model : Link function, logit, probit, complementary log-log, estimation of parameters, odds ratio, hypothesis testing using model deviance.

### **Books recommended**

1. Jean Gomes : Leading in nonlinear world : Building Wellbeing, strategic and innovation mindsets for the future
2. S. Nanda : Nonlinear Analysis
3. Steen Krenk: Non linear Modelling Cambridge
4. Giuseppe Lancia, Paolo Serafini : Compact Extended Linear Programming Models  
springer

### DSEI.3: Operations Research

#### Course Objectives:

Operations research deals with the application of advanced analytical methods which helps in taking better decisions. The course includes advanced techniques that are useful in business, management, industry, project planning etc.

#### Course Outcomes:

At the end of the course, students become well versed with,

1. Concept of inventory problem, need of inventory and types of inventory models and types of probabilistic inventory models.
2. Sequencing problems and methods to solve sequencing problems in different situations
3. Concept of queues, different types of queues and their analysis.
4. Concept of Networking, CPM, PERT and methods of obtaining optimum solution to the problems.

**Unit I : Inventory problems** : Structure of inventory problem, EOQ formula, EOQ model with uniform rate of demand & having no shortages, EOQ model with different rate of demand in different cycles having no shortages, EOQ model with uniform rate of demand & finite rate of replenishment having no shortages, EOQ model with uniform rate of demand & finite rate of replenishment having shortages, EOQ model with uniform rate of demand, infinite rate of replenishment having shortages, EOQ model with single & double price breaks.

**Unit II** : Single period probabilistic inventory models with

- i) instantaneous demand & discrete units
- ii) instantaneous demand & continuous units
- iii) Continuous demand & discrete units
- iv) Continuous demand & continuous units

**Unit III** : Processing n jobs through two machines,

Processing n jobs through three machines,

Processing 2 jobs through m machines,

Processing n jobs through m machines,

Traveling salesman problem

Queuing Models:  $M/M/1$  : FCFS /  $\infty$  /  $\infty$  & its generalization

$M/M/1$ : FCFS /  $N/M/M/C$  ,

FCFS /  $M/E_k/1$ : FCFS /  $\infty / \infty$ ,

$II / II$  ,

**Unit IV** : Networking : Basic steps in PERT & CPM, methods of solving PERTproblem, crashingthe network, updating (PERT & CPM) max. flow min. cut theorem, problems based on max.flowmin.cuttheorem.

**Books Recomonded**

1. S. Kalavathy : Operations Research Vikas Publications
2. Frederick S. Hillier : An introduction to Operations Research McGraw Hill
3. Kantiswaroop, P. K. Gupta, Man Mohan : Operations Research Sultan Chand & Sons
4. SheikhAhmedHossain, SamarjitKar : Operations Research Recent Advances Narosa Publishing House

**DSE II.3 : Bioassay**

**Course Objectives:**

Bioassay is an analytical method to determine concentration of a substance by its effect on living cells, tissues, insects, etc. There are various types of Bioassays like qualitative or quantitative, direct or indirect. These analytical methods are useful in environmental science, microbiology etc. The method of dose and response relationship in this analysis is used in pharmaceutical sciences. Objective of this course is to train students in analytical methods used in these fields.

### **Course Outcomes:**

**At the end of the course, students become well versed with,**

1. Types of biological assays and methods for estimating dose response relationship.
2. Logit and probit approach for estimating dose-response relationship.
3. Methods of estimation of parameters and dose allocation schemes.
4. Sequential procedures, estimation of safe dose, ANOVA and Bayesian approach to Bioassays.

**Unit I :** Types of biological assays, Direct assays, ratio estimators, asymptotic distributions, Fieller's theorem. Regression approaches to estimating dose-response relationships, Logit and Probit approaches when dose-response curve for standard preparation is unknown.

**Unit II :** Methods of estimation of parameters, estimation of extreme quantiles., dose allocation schemes. Quantal Responses, Polychotomous quantal responses. estimation of points on the quantal response function

**Unit III :** Sequential procedures, estimation of safe doses.

**Unit IV :** ANOVA and Bayesian approach to Bioassay

### **Books Recommended**

1. R.C. Dubey : Advanced Biotechnology S. Chand
2. S.J. Amdekar : Statistical Methods for Agricultural and Biological sciences
3. P.K. Bajpai : Biological instrumentation and Methodology S. Chand & Company
4. Thieman : Introduction to Biotechnology Pearson

## DSE III.3 : Econometrics

### Course Objective

The purpose of this course is to give students a solid foundation in econometric techniques, various functions for economic analysis and future forecasting.

### Course Outcomes

On completion of this course, students will be able to:

- 1: Understand the basic concepts of econometric models.
- 2: Learn knowledge of various econometric models, estimation methods and related econometric theories.
- 3: Understand the statistical techniques to model relationships between variables and make predictions.
- 4: Learn how to conduct econometric analysis of data.

**Unit I :** Introduction to econometrics. A review of least squares and maximum likelihood estimation methods of parameters in classical linear regression model and their properties. Generalized least squares estimation and prediction, construction of confidence regions and tests of hypotheses. Regression analysis under linear restrictions, restricted least squares estimation method and its properties. Autocorrelation, sources and consequences, Autoregressive process tests for autocorrelation, Durbin Watson test.

### Unit

### II

: Problem of Multicollinearity, its implications. Source of multicollinearity, tools for handling the problem of multicollinearity. Remedies for multicollinearity. Ridge regression. Heteroskedasticity, consequences and tests for it, estimation procedures under heteroskedastic disturbances, Bartlett's test, Breusch-Pagan test and Goldfeld-Quandt test. Dummy Variable Models.

**Unit III :** Specification Error Analysis, Tests for Structural Change and Stability, Asymptotic theory and regressors. Stein-Rule Estimation. Instrumental variable estimation. Measurement Error Models.

**Unit IV :** Simultaneous equations model, problem of identification, necessary and sufficient condition for the identifiability of parameters in a structural equation, ordinary least squares, indirect least squares, two-stage least squares and limited information maximum likelihood method.

### Books Recommended

1. Gujarati, D.N. & Porter, D.C. (2017). Basic Econometrics, 6<sup>th</sup> Edition. McGraw Hill.
2. Maddala, G.S. & Lahiri, K. (2010). Introduction to Econometrics, 4<sup>th</sup> Edition. Wiley.
3. Greene, W.H. (2012). Econometric Analysis, 7<sup>th</sup> Edition. Pearson.
- Studenmund, A.H. & Johnson, B.K. (2017). Using Econometrics: A Practical Guide, 7<sup>th</sup> Edition. Pearson.

### DSE IV.3: Actuarial Statistics

#### Course Objectives:

Actuarial science includes statistical methods to assess risk mainly in insurance and finance. The course includes these statistical methods based on probability theory and stochastic models. Objective here is to make the students aware about this important branch of statistics.

#### Course Outcomes:

At the end of the course, students become well versed with,

1. Concept of inventory problem, need of inventory and types of inventory models and types of probabilistic inventory models.
2. Sequencing problems and methods to solve sequencing problems in different situations
3. Concept of queues, different types of queues and their analysis.
4. Concept of Networking, CPM, PERT and methods of obtaining optimum solution to the problems.

**Unit I :** Life table and its relation with survival function, assumptions for fractional ages, some analytical laws of mortality, select and ultimate tables. Multiple life functions, joint and last survivor status, insurance and annuity benefits through multiple life functions. Multiple decrement models, deterministic and random survivor groups, associated single decrement tables, central rates of multiple decrement, net single premiums and their numerical evaluations.

#### Unit

#### II

: Principles of compound interest: Nominal and effective rates of interest and discount, force of interest and discount, compound interest, accumulation factor, continuous compounding. Life insurance : Insurance payable at the moment of death and at the end of the year of death-level benefit insurance, endowment insurance, deferred insurance and varying benefit insurance, recursion, commutation functions.

**Unit III :** Life annuities : Single payment, continuous life annuities, discrete life annuities, life annuities with monthly payments, commutation functions, varying annuities, recursion, complete annuities-immediate and apportionable annuities-due. Net premiums : Continuous and discrete premiums, true monthly payments premiums, apportionable premiums, commutation functions, accumulation type benefits.



**Unit IV:** Netpremium reserves:Continuousanddiscrete netpremium reserveson a semicontinuous basis, reserves based on true monthly premiums, reserves on an apportionable ordiscountedcontinuousbasis,reservesatfractionalduration,allocationsoflosstopolicyyears,recursiveformul as and differential equationsfor reserves, commutation functions. Somepracticalconsiderations:Premiumsthatincludeexpenses–generalexpenses,typesofexpenses, per policy expenses. Claim amount distributions, approximating the individualmodel,stop-lossinsurance.

**Books Recomended**

1. Shailaja R. Deshmukh : Actuarial Statistics An introduction Universities Press ( India )
2. Dale S. Borowiak, Arnold F Shapiro : Financial and Actuarial Statistics Chapman and Hall
3. P. S. Waldhe : Actuarial Statistics NiraliPrakashan
4. Swiss Re : Statistical foundations of Actuarial Learning and its applications Springer

**LABI :Practicals Based on DSCI.3 and DSCII.3**

**LABII :Practicals Based on DSCIII.3 and DSEI.3**

## M.Sc. II (Statistics)(NEP Pattern) SIV

### DSCI.4: Computational Statistics

#### Course Objectives:

In many disciplines, results are established with the help of the data by fitting a suitable model. Analyzing the data plays an important role in such cases. Advanced statistical methods and different types of models can be applied to these data, even very big data. The course deals with different computational methods and algorithms necessary for analysis of the data. The course includes different methods that are particularly useful in simulating data from various distributions and analyzing them with the help of computers.

#### Course Outcomes:

At the end of the course, students become well versed with,

1. Visualization of data and exploratory data analysis.
2. Stochastic simulation techniques like MCMC.
3. Some important methods of handling missing data and incomplete data problems like EM algorithm etc.
4. Jackknife, Bootstrap and nonparametric density estimation using kernels.

#### Unit

I

: Exploratory data analysis: Components of EDA, transforming data, Clustering: Similarity measures, similarity coefficients, Hierarchical

clustering methods: single, complete and average linkage methods, dendrograms. Graphical Methods: Quintile plots, Box Plots, Histogram, Stem & leaf diagram, Q-Q plots, P-P plots

**Unit II** : Stochastic simulation: generating random variables from discrete and continuous distributions, simulation bivariate/multivariate distributions, simulating stochastic processes such as simple queues. Variance reduction technique: Importance sampling for integration, control variates, antithetic variables. MCMC methods : Essence of MCMC methods, Time reversible MC, Law of large numbers for MC. Metropolis-Hastings algorithm, Gibbs sampling for bivariate/multivariate simulation.

Simulated annealing for optimization, simulated annealing for M.C. Simulation based testing: simulating test statistics and power functions, permutation/randomization tests.

**Unit III** : Resampling paradigms: Jackknife and Bootstrap: Delete one J-K, pseudo values, Bias and S.E. Efron's bootstrap, Bootstrap C.I. Bootstrap-t C.I., Bootstrap C.I. (percentile

method), Bootstrap in regression, Bootstrap C.I. for linear regression parameters.

**Unit IV** : EM algorithm: Application to missing and incomplete data problems. Mixture models. Smoothing with Kernels: Density estimation, kernel density estimator for univariate data, Bandwidth selection and cross validation, Max likelihood LCV, Least square CV.

### **Books Recommended**

1. J. E. Gentle, W. K. Hardle, Y. Mori : Computational Statistics Concepts and Methods Springer
2. G.H. Givens, J.A. Hoeting : Computational Statistics Wiley
3. J.E. Gentle : Statistics and Computing Springer
4. R.L. Ruiz : Computational Statistics and Applications
5. Marepalli Rao, C.R. Rao : Computational Statistics with R Elsevier

## M.Sc. II (Statistics)(NEP Pattern) SIV

### DSCII.4 : Multivariate Analysis

#### Course Objective

The main objective of this course is to introduce students to the analysis of observations on several correlated random variables for a number of individuals. Multivariate analysis is applicable in almost all scientific studies, for example in Anthropology, Life sciences, Agriculture and Economics, when one deals with several variables simultaneously.

#### Course Outcome

After completing this course, student is expected to learn the following:

- 1 Account for important theorems and concepts in multivariate analysis.
- 2 Understand the concept of Wishart and Hotelling's  $T^2$  distribution.
- 3 Understand the link between multivariate techniques and corresponding univariate techniques.
- 4 Conduct statistical inference about multivariate means including hypothesis testing, confidence region calculation, etc

**Unit I** : Multivariate normal distribution, its properties and characterization. Random sampling from a multivariate normal distribution. Maximum likelihood estimator of parameters. Distribution of sample mean vector. Inference concerning the mean vector when the covariance matrix is known. Matrix normal distribution. Multivariate central limit theorem.

**Unit II** : Wishart matrix, its distribution and properties. Distribution of sample generalized variance. Hotelling's  $T^2$  statistic and its distribution and properties. Applications in tests on mean vector for one and more multivariate normal populations. Mahalanobis'  $D^2$ .

**Unit III** : Likelihood ratio test criteria for testing of independence of set of variables, equality of covariance matrices, identity of several multivariate normal populations, equality of a covariance matrix to a given matrix, equality of a mean vector and a covariance matrix to a given vector and a given matrix

**Unit IV** : Classification and discrimination procedures for discrimination between two multivariate normal populations, sample discriminant function, tests associated with discriminant functions, classification into more than two multivariate normal populations. Principal

components, canonical variables and canonical correlations. Multivariate analysis of variance [MANOVA] of one-way classified data. Wilk's lambda criterion.

### **Books Recommended**

1. Johnson, R. A. and Wichern, D. W. (2015): Applied Multivariate Statistical Analysis, Sixth Edition, Pearson Education India.
2. Härdle, W. K. and Hlavka, Z. (2015): Multivariate Statistics, Springer.
3. Anderson, T. W. (2003): An Introduction to Multivariate Statistical Analysis, Third Edition, Wiley.
4. Härdle, W. K. and Simar, L. (2015): Applied Multivariate Statistical Analysis, Springer.
- Singh, B. M. (2004): Multivariate statistical analysis, South Asian Publishers.

## M.Sc. II (Statistics)(NEP Pattern) SIV

### DSCIII.4 : Stochastic Process

#### Course Objective

The objective of this course is to apprise the students with the basic concepts of the theory of stochastic processes in continuous time, also to make them able to use various analytical and computational techniques to study stochastic models that appear in applications.

#### Course Outcomes

After completing this course, student is expected to learn the following:

- 1 Study the fundamental concept of stochastic processes and its applications.
- 2 Understand Markov processes and Markov chains and their applications in real world.
- 3 Study the branching process and its properties.
- 4 Understand Poisson processes and its variations.

**Unit I** : Stochastic Processes: Introduction, classification according to state space and time domain. Countable state Markov chains, transition probability matrix, Chapman-Kolmogorov equations, calculation of  $n$ -step transition probabilities and their limits, stationary distribution.

**Unit II** : Branching Processes: Properties of generating function of branching processes, probability of ultimate extinction, distribution of the total number of progeny, generalization of the classical Galton-Watson branching process, general branching processes, random walk and gambler's ruin problem.

**Unit III** : Continuous-time Markov Processes: Poisson process and related distributions, generalizations of Poisson process, simple birth-process, simple death-process, simple birth-death process, linear birth-death process. First passage time distribution.

**Unit IV** : Renewal Theory: Elementary renewal theorem and applications. Statement and uses of key renewal theorem, central limit theorem for renewals, study of residual and excess lifetime's process. Renewal reward Process, Markov renewal and semi-Markov processes, Markov renewal equations.

#### Books Recommended

1. Medhi, J. (2012). Stochastic Processes, 3<sup>rd</sup> Edition. New Age International.
2. Ross, S.M. (2016). Stochastic Processes, 2<sup>nd</sup> Edition. Wiley India.

3. Karlin, S. & Taylor, H.M. (2012). A First Course in Stochastic Processes, 2<sup>nd</sup> Edition. Academic Press.
4. Prabhu, N.U. (2010). Stochastic Processes: Basic Theory and its Applications. World Scientific.

## M.Sc. II (Statistics)(NEP Pattern) SIV

### DSEI.4: Bayesian Inference

#### Course Objective

The objective of this course is to provide the understanding of the decision theory and fundamentals of Bayesian inference including concept of subjectivity and priors by examining some simple Bayesian framework.

#### Course Outcomes

After successful completion of this course, student will be able to:

1. To understand and utilize past experience along with present observation and improve the inferences.
2. Equip students with skills to carry out and interpret posterior data-based modeling and analyses.
3. Understand Decision theoretical concepts, game theory and their applications.
4. To understand the Bayesian estimation and testing procedures and compare them with classic inference.

**Unit I** : Bayes Rule, extended Bayes rule, Minimax rule, methods for finding minimax rules, Generalized bayes and limit of bayes rule, Concept of admissibility and completeness Bayes rules, Admissibility of Bayes and minimax rules, Supporting and separating hyper plane theorems, complete class theorem, Minimax estimators of Normal and Poisson means.

**Unit II** : Subjective interpretation of probability in terms of fair odds, Evaluation of (i) subjective probability of an event using a subjectively unbiased coin (ii) subjective prior distribution of a parameter, Bayes theorem and computation of the posterior distribution, Natural Conjugate family of priors for a model, Hyperparameters of a prior from conjugate family

**Unit III** : Bayesian point estimation as a prediction problem from posterior distribution, Bayes estimators for (i) absolute error loss (ii) squared error loss (iii) 0 -1 loss, Bayesian interval estimation: credible intervals, Highest posterior density regions

**Unit****IV**

:

Interpretation of the confidence coefficient of an interval and its comparison with the interpretation of the confidence coefficient for a classical confidence interval, Bayesian Testing Hypothesis: Specification of the appropriate form of the prior distribution for a Bayesian testing of hypothesis problem, Prior odds, Posterior odds, Bayes factor.

**Books Recommended**

1. James O Berger (1985): Statistical Decision Theory and Bayesian analysis. Springer.
2. Ferguson T.S. (1967): Mathematical Statistics - A decision theoretic Approach. Academic Press.
3. DeGroot. M.H. : Optimal Statistical Decisions. McGraw Hill.
4. Leonard T and Hsu J.S.J.: Bayesian Methods. Cambridge University Press.
5. Bernardo, J.M. and Smith AFM: Bayesian Theory. John Willey.
6. Rao, C. R. (1973): Linear Statistical Inference and its Applications, Wiley Eastern.
7. Robert, C.P.: The Bayesian Choice: A Decision Theoretic Motivation, Springer



## **M.Sc. II (Statistics)(NEP Pattern) SIV**

### **DSEII.4 : Statistical Ecology**

#### **Course Objectives:**

Ecology is study of interaction of organisms that include biotic and abiotic components and their environment. Ecologists can explain life processes, interactions, adaptations, movement of materials, distribution of organisms, biodiversity etc. by using various statistical methods. The course gives knowledge of these methods and models in this particular branch.

#### **Course Outcomes:**

**At the end of the course, students become well versed with,**

1. Concept of inventory problem, need of inventory and types of inventory models and types of probabilistic inventory models.
2. Sequencing problems and methods to solve sequencing problems in different situations
3. Concept of queues, different types of queues and their analysis.
4. Concept of Networking, CPM, PERT and methods of obtaining optimum solution to the problems.

**Unit I :** Population Dynamics One species exponential, logistic and Gompertz models, Two species competition, coexistence, predator-prey oscillation, Lotka-Volterra Equations, isoclines, Leslie matrix model for age structured populations. Survivorship curves constant hazard rate, monotone hazard rate and bathtub shaped hazard rates

**Unit II :** Population density estimation: Capture recapture models, nearest neighbor models, Line transect sampling, Ecological Diversity, Simpson's index, Diversity as a measure of rarity

**Unit III :** Optimal Harvesting of Natural Resources, Maximum Sustainable yield, tragedy of the commons Game theory in ecology, concepts of Evolutionarily stable strategy, its Properties, simple cases such as Hawk-Dove game.

**Unit IV** : Foraging Theory: Diet choice Problem, patch choice problem, mean variance tradeoff.

**Books Recommended**

1. L.J. Young , J. H. Young : Statistical Ecology Springer
2. D.I. Warton : Data analysis in Ecology Springer
3. A. P. Robinson , S.T. Buckland, P. Reich M. McCarthy : Methods in statistical Ecology Springer
4. G. Guillot, A. Arab, J. B. Illian, S Dray : Advances in statistical Ecology

## DSEIII.4: Regression Analysis

### Course Objective

The objectives of this course are to develop theoretical foundation of regression models and understand fundamental concepts of regression analysis.

### Course Outcome

On completion of this course, students will be able to:

- 1 Understand simple and multiple linear regression models with their applications.
- 2 Learn the fitting of these models to simulated and real datasets.
- 3 Learn model adequacy using classical diagnostics, awareness of potential problems (outliers, etc.) and application of remedies to deal with them.
- 4 Understand the basic concepts of logistic, Poisson and generalized linear models.

**Unit I :** Simple Linear Regression: Simple linear regression model. Least-square estimation of parameters. Hypothesis testing on the slope and intercept. Interval estimation in simple linear regression. Prediction of new observations. Coefficient of determination. Estimation by maximum likelihood. Multiple linear regression: Multiple linear regression models. Estimation of the model parameters. Hypothesis testing in multiple linear regression. Confidence intervals in multiple regression. Coefficient of determination and Adjusted  $R^2$ .

**Unit II :** Model Adequacy: Checking of linearity between study and explanatory variable, Residual Analysis, Detection and treatment of outliers, Residual plots. The PRESS statistic. Outlier test based on Studentized Residual (R-student). Test for lack of fit of the regression model. Transformation and Weighting to Correct Model Inadequacies: Variance stabilizing transformations. Transformation to linearize the model. Analytical methods for selecting a transformation on study variable.

**Unit III :** Generalized and weighted least square estimation. Polynomial Regression Models: Polynomial model in one variable. Orthogonal Polynomials. Piecewise polynomial (Splines). Variable Selection and M

odelBuilding:Incorrectmodelspecifications.Evaluationofsubset regressionmodel.Computationaltechniquesforvariableselection.

**Unit IV** : Logistic and Poisson regression models: Introduction, Linear predictorandlinkfunctions,logit,probit,oddsratio,maximumlikelihoodestimation, test of hypothesis. Generalized linear models: Exponentialfamily of distribution, Linear predictors and link functions, MaximumlikelihoodestimationofGLM.Predictionandconfidenceintervalwith GLM.

### **Books Recomonded**

1. Montgomery,D.C.,Peck,E.A.&Vining,G.G.(2015).IntroductiontoLinearRegressionAnalysis,5<sup>th</sup>Edition.Wiley.
  2. Rao,C.R.(2009).LinearStatisticalInferenceanditsApplications,2<sup>nd</sup>Edition.Wiley.
  3. Draper,N.R.&Smith,H.(2011).AppliedRegressionAnalysis,3<sup>rd</sup> Edition.Wiley.
  4. Chatterjee, S.andHadi,A.S.(2012).RegressionAnalysisbyExample,5<sup>th</sup>Edition.Wiley.
- Fox,J.andWeisberg,S.(2019).AnRCompanionto AppliedRegression,3<sup>rd</sup> Edition.SagePublications

## M.Sc. II (Statistics)(NEP Pattern) SIV

### DSE IV.4 : Reliability Theory

#### Course Objectives:

Manmadesystemssufferfromimperfectionsforseveralreasons.Oftentheseimperfections leadto improper functioning resulting infailure of the systemIt maybe the result of defect in the system while producing it or may be because of naturalcomponent deterioration on some interacting factors. Probability of non failure istermed as reliability. Reliability models can be developed for predicting the reliabilityofacomponentorofsystempriortoitsimplementation.

#### Course Outcomes:

**At theend ofthecourse,studentsbecomewellversed with,**

1. Failuretimedistribution, reliabilityfunction, hazardfunctionetc.
2. Increasingfailurerateasaneffectofageing, shockmodels.
3. Reliabilityestimationinvariouscases.
4. Reliabilitygrowthmodels.

**Unit I :** Reliability concepts and measures ,components and systems, coherent systems, reliabilityof coherent systems, cuts and paths, modular compositions, bounds on system reliability,structural and reliability importance of components. Life distributions, reliability functions,hazardrate,commonlifedistributions,exponential,Gamma,Weibull,Lognormaletc.Est imationofparameters, confidenceintervals,LRandMLEtestsforthesedistributions.

**Unit II :** Notions of ageing: IFR, IFRA, NBU, DMRL and NBUE classes and their duals, loss ofmemory property of the exponential distribution, closures of these classes under formation ofcoherentsystems,convolutionsandmixtures.Univariate shockmodelsandlifedistributions arisingoutofthem,bivariate shockmodel,commonbivariateexponentialdistributionsandtheirpropert

ies.

**Unit III** : Reliability estimation based on failure times in variously censored life tests and in tests with replacement of failed items, stress and strength reliability and its estimation. Maintenance and replacement policies, availability of repairable systems, modeling of repairable system by a non-homogeneous Poisson process

**Unit IV** : Reliability growth models, probability plotting techniques, Hollander-Proschan and Deshpande tests for exponentially, tests for HPP vs. NHPP with repairable systems.

**Books Recommended**

1. M. Rausand, A. Barros, A. Hoyland : System Reliability Theory Wiley
2. I. Bazovsky : Reliability Theory and Practice Dover Publications
3. J. Navarro: Introduction to system Reliability Theory Springer
4. B.V. Gnedenko : Mathematical methods of reliability theory Academic Press

**M.Sc. II (Statistics)(NEP Pattern) SIV**

**LAB I : Practical based on DSCI.4 & DSC II.4**

**LAB II - Practical based on DSC III.4 & DSE I.4**